

smallantimagmas

**A library of antiassociative magmas of
small order**

0.3.0

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Contents

- 1 smallantimagmas automatic generated documentation 4**
- 1.1 smallantimagmas automatic generated documentation of properties 4
- 1.2 smallantimagmas automatic generated documentation of attributes 7
- 1.3 smallantimagmas automatic generated documentation of global functions 9
- 1.4 smallantimagmas automatic generated documentation of methods 12

- Index 14**

Chapter 1

smallantimagmas automatic generated documentation

1.1 smallantimagmas automatic generated documentation of properties

1.1.1 IsAntiassociative (for IsMagma)

▷ `IsAntiassociative(M)` (property)

Returns: true or false

identifies whether magma M is antiassociative.

Example

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.1.2 IsLeftCyclic (for IsMagma)

▷ `IsLeftCyclic(M)` (property)

Returns: true or false

if magma is left cyclic m .

1.1.3 IsRightCyclic (for IsMagma)

▷ `IsRightCyclic(M)` (property)

Returns: true or false

if magma is left cyclic m .

1.1.4 IsLeftCancellative (for IsMagma)

▷ `IsLeftCancellative(M)` (property)

Returns: true or false

if magma is left cancellative m .

Example

```

gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display( MultiplicationTable(M) );
[ [ 2, 1 ],
  [ 2, 1 ] ]
gap> IsRightCancellative(M);
false
gap> IsLeftCancellative(M);
true
gap> List(AllSmallAntimagmas(2), M -> IsLeftCancellative(M));
[ true, false ]

```

1.1.5 IsRightCancellative (for IsMagma)

▷ `IsRightCancellative(M)` (property)

Returns: true or false
if magma is right cancellative m .

Example

```

gap> List(AllSmallAntimagmas(2), M -> IsRightCancellative(M));
[ false, true ]

```

1.1.6 IsCancellative (for IsMagma)

▷ `IsCancellative(M)` (property)

Returns: true or false
if magma is cancellative m .

Example

```

gap> List(AllSmallAntimagmas(2), M -> IsCancellative(M));
[ false, false ]

```

1.1.7 IsLeftFPFInducted (for IsMagma)

▷ `IsLeftFPFInducted(M)` (property)

Returns: true or false
is a left-hand sided fixed-point free inducted m .

Example

```

gap> Display( MultiplicationTable( SmallAntimagma(2, 2) ) );
[ [ 2, 2 ],
  [ 1, 1 ] ]
gap> IsLeftFPFInducted( SmallAntimagma(2, 2) );
true

```

1.1.8 IsRightFPFInducted (for IsMagma)

▷ `IsRightFPFInducted(M)` (property)

Returns: true or false
is a right-hand sided fixed-point free inducted m .

Example

```
gap> Display( MultiplicationTable( SmallAntimagma(2, 1) ) );
[ [ 2, 1 ],
  [ 2, 1 ] ]
gap> IsRightFPFInducted( SmallAntimagma(2, 1) );
true
```

1.1.9 IsLeftDerangementInducted (for IsMagma)

▷ `IsLeftDerangementInducted(M)` (property)

Returns: true or false

is a left-hand sided derangement inducted m .

Example

```
gap> M := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> IsLeftFPFInducted(M);
true
gap> IsRightFPFInducted(M);
false
gap> IsRightDerangementInducted(M);
false
```

1.1.10 IsRightDerangementInducted (for IsMagma)

▷ `IsRightDerangementInducted(M)` (property)

Returns: true or false

is a right-hand sided derangement inducted m .

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> IsLeftFPFInducted(M);
false
gap> IsRightFPFInducted(M);
true
gap> IsRightDerangementInducted(M);
true
```

1.1.11 IsLeftAlternative (for IsMagma)

▷ `IsLeftAlternative(M)` (property)

Returns: true or false

is a left-alternative magma M .

Example

1.1.12 IsRightAlternative (for IsMagma)

▷ `IsRightAlternative(M)` (property)

Returns: true or false

is a right-alternative magma M .

Example

1.2 smallantimagnas automatic generated documentation of attributes

1.2.1 AssociativityIndex (for IsMagma)

▷ AssociativityIndex(M) (attribute)

identifies associativity index of M .

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>
gap> AssociativityIndex(OneSmallAntimagma(2));
0
gap> OneSmallGroup(4);
<pc group of size 4 with 2 generators>
gap> AssociativityIndex(OneSmallGroup(4));
64
gap> AssociativityIndex(OneSmallGroup(4)) = 4 ^ 3;
true
```

1.2.2 DiagonalOfMultiplicationTable (for IsMagma)

▷ DiagonalOfMultiplicationTable(M) (attribute)

computes diaognal of multiplication table of M .

Example

```
gap> List(AllSmallAntimagnas(3), M -> DiagonalOfMultiplicationTable((M)));
[ [ 2, 1, 1 ], [ 2, 1, 1 ],
  [ 2, 3, 2 ], [ 2, 1, 1 ],
  [ 2, 1, 1 ], [ 2, 1, 2 ],
  [ 2, 3, 2 ], [ 2, 1, 2 ],
  [ 2, 3, 1 ], [ 2, 3, 1 ]
]
```

1.2.3 CommutativityIndex (for IsMagma)

▷ CommutativityIndex(M) (attribute)

identifies commutativity index of M .

Example

1.2.4 AnticommutativityIndex (for IsMagma)

▷ AnticommutativityIndex(M) (attribute)

calculates anticommutativity index of M .

Example

1.2.5 SquaresIndex (for IsMagma)

▷ SquaresIndex(M) (attribute)

computes squares index of M so the order of $\{m^2 | m \in M\}$.

Example

```
gap> List(AllSmallAntimagmas(2), M -> List(M, m -> m * m));
[ [ m2, m1 ], [ m2, m1 ] ]
gap> List(AllSmallAntimagmas(2), M -> SquaresIndex(M));
[ 2, 2 ]
gap> List(AllSmallAntimagmas(3), M -> SquaresIndex(M));
[ 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 3 ]
```

1.2.6 IdSmallAntimagma (for IsMagma)

▷ IdSmallAntimagma(M) (attribute)

identifies class of antiassociative magma M .

Example

```
gap> IsAntiassociative(OneSmallGroup(16));
false
gap> IsAntiassociative(OneSmallAntimagma(2));
true
gap> IsAntiassociative(OneSmallAntimagma(3));
true
```

1.2.7 LeftOrder (for IsExtLElement)

▷ LeftOrder($[m]$) (attribute)

returns a left order of element m .

1.2.8 RightOrder (for IsExtRElement)

▷ RightOrder($[m]$) (attribute)

returns a right order of element m .

1.2.9 LeftOrdersOfElements (for IsMagma)

▷ LeftOrdersOfElements($[m]$) (attribute)

returns a left order of element m .

1.2.10 RightOrdersOfElements (for IsMagma)

▷ RightOrdersOfElements($[m]$) (attribute)

returns a left order of element m .

1.3 smallantimagmas automatic generated documentation of global functions

1.3.1 AllSubmagmas

▷ AllSubmagmas(M) (function)

builds a collection of non-isomorphic submagmas of M .

Example

```
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> List(AllSmallAntimagmas(2), M -> AllSubmagmas(M));
[ [ <magma with 1 generator> ], [ <magma with 1 generator> ] ]
```

1.3.2 MagmaIsomorphismInvariantsMatch

▷ MagmaIsomorphismInvariantsMatch(M) (function)

computes isomorphism invariants of M .

1.3.3 IsMagmaIsomorphic

▷ IsMagmaIsomorphic(M, N) (function)

identifies whether magmas M, N are isomorphic.

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> T := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> IsMagmaIsomorphic(M, M);
true
gap> IsMagmaIsomorphic(M, T);
true
gap> IsMagmaIsomorphic(M, N);
false
```

1.3.4 IsMagmaAntiisomorphic

▷ IsMagmaAntiisomorphic($[M, N]$) (function)

identifies whether magmas M, N are antiisomorphic.

Example

```
gap> N := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
```

```

gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, M);
false
gap> IsMagmaAntiisomorphic(M, N);
true
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true

```

1.3.5 TransposedMagma

▷ `TransposedMagma([M])` (function)

generates transposed magma M .

Example

```

gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> IsMagmaAntiisomorphic(M, TransposedMagma(M));
true
gap> IsMagmaIsomorphic(M, TransposedMagma(TransposedMagma(M)));
true
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> Display(MultiplicationTable(M));
[ [ 2, 1 ],
  [ 2, 1 ] ]
gap> Display(MultiplicationTable(TransposedMagma(M)));
[ [ 2, 2 ],
  [ 1, 1 ] ]

```

1.3.6 LeftPower

▷ `LeftPower([m, k])` (function)

returns a left k -power of element m .

1.3.7 RightPower

▷ `RightPower([m, k])` (function)

returns a right k -power of element m .

1.3.8 AllSmallAntimagmas

▷ `AllSmallAntimagmas(n)` (function)

returns all antiassociative magmas of specified size n (a number)

Example

```
gap> AllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
gap> AllSmallAntimagmas(3);
[
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>,
  <magma with 3 generators>, <magma with 3 generators>
]
```

1.3.9 NrSmallAntimagmas

▷ NrSmallAntimagmas(n) (function)

counts number of antiassociative magmas of specified size n (a number).

Example

```
gap> NrSmallAntimagmas(2);
2
gap> NrSmallAntimagmas(3);
10
gap> NrSmallAntimagmas(4);
17780
```

1.3.10 SmallAntimagma

▷ SmallAntimagma(n, i) (function)

returns antiassociative magma of id $[n, i]$.

Example

```
gap> SmallAntimagma(2, 1);
<magma with 2 generators>
gap> SmallAntimagma(4, 5);
<magma with 4 generators>
```

1.3.11 OneSmallAntimagma

▷ OneSmallAntimagma(n) (function)

returns a random antiassociative magma of size n .

Example

```
gap> OneSmallAntimagma(2);
<magma with 2 generators>

gap> OneSmallAntimagma(3);
<magma with 3 generators>
```

1.3.12 ReallyAllSmallAntimagmas

▷ ReallyAllSmallAntimagmas(n) (function)

returns really-all antiassociative magmas, isomorphic, of specified size n (a number)

Example

```
gap> ReallyAllSmallAntimagmas(2);
[ <magma with 2 generators>, <magma with 2 generators> ]
```

1.3.13 ReallyNrSmallAntimagmas

▷ ReallyNrSmallAntimagmas(n) (function)

counts number of antiassociative magmas of specified size n (a number)

Example

```
gap> ReallyNrSmallAntimagmas(3);
52
```

1.3.14 AntimagmaGeneratorPossibleDiagonals

▷ AntimagmaGeneratorPossibleDiagonals(n) (function)

returns all possible diagonals of multiplication table for $[n]$ -antimagma.

Example

```
gap> AntimagmaGeneratorPossibleDiagonals(2);
[ [ 2, 1 ] ]
gap> AntimagmaGeneratorPossibleDiagonals(3);
[
  [ 2, 1, 1 ], [ 2, 1, 2 ], [ 2, 3, 1 ], [ 2, 3, 2 ],
  [ 3, 1, 1 ], [ 3, 1, 2 ], [ 3, 3, 1 ], [ 3, 3, 2 ]
]
```

1.3.15 AntimagmaGeneratorFilterNonIsomorphicMagmas

▷ AntimagmaGeneratorFilterNonIsomorphicMagmas(Ms) (function)

filters non-isomorphic magmas m .

1.4 smallantimagmas automatic generated documentation of methods

1.4.1 MagmaIsomorphism (for IsMagma, IsMagma)

▷ MagmaIsomorphism(M, N) (operation)

computes an isomorphism between magmas M, N .

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := MagmaByMultiplicationTable([ [2, 1], [2, 1] ]);
<magma with 2 generators>
gap> MagmaIsomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

1.4.2 MagmaAntiisomorphism (for IsMagma, IsMagma)

▷ MagmaAntiisomorphism(M , N)

(operation)

creates an antiisomorphism between magmas M , N .

Example

```
gap> M := SmallAntimagma(2, 1);
<magma with 2 generators>
gap> N := SmallAntimagma(2, 2);
<magma with 2 generators>
gap> MagmaAntiisomorphism(M, N);
<mapping: Domain([ m1, m2 ]) -> Domain([ m1, m2 ]) >
```

Index

AllSmallAntimagmas, 10
AllSubmagmas, 9
AnticommutativityIndex
 for IsMagma, 7
AntimagmaGeneratorFilterNonIsomorphic-
 Magma, 12
AntimagmaGeneratorPossibleDiagonals, 12
AssociativityIndex
 for IsMagma, 7

CommutativityIndex
 for IsMagma, 7

DiagonalOfMultiplicationTable
 for IsMagma, 7

IdSmallAntimagma
 for IsMagma, 8
IsAntiassociative
 for IsMagma, 4
IsCancellative
 for IsMagma, 5
IsLeftAlternative
 for IsMagma, 6
IsLeftCancellative
 for IsMagma, 4
IsLeftCyclic
 for IsMagma, 4
IsLeftDerangementInducted
 for IsMagma, 6
IsLeftFPFInducted
 for IsMagma, 5
IsMagmaAntiisomorphic, 9
IsMagmaIsomorphic, 9
IsRightAlternative
 for IsMagma, 6
IsRightCancellative
 for IsMagma, 5
IsRightCyclic
 for IsMagma, 4

IsRightDerangementInducted
 for IsMagma, 6
IsRightFPFInducted
 for IsMagma, 5

LeftOrder
 for IsExtLElement, 8
LeftOrdersOfElements
 for IsMagma, 8
LeftPower, 10
License, 2

MagmaAntiisomorphism
 for IsMagma, IsMagma, 13
MagmaIsomorphism
 for IsMagma, IsMagma, 12
MagmaIsomorphismInvariantsMatch, 9

NrSmallAntimagmas, 11

OneSmallAntimagma, 11

ReallyAllSmallAntimagmas, 12
ReallyNrSmallAntimagmas, 12
RightOrder
 for IsExtRElement, 8
RightOrdersOfElements
 for IsMagma, 8
RightPower, 10

SmallAntimagma, 11
SquaresIndex
 for IsMagma, 8

TransposedMagma, 10